

# GENERALIZABILITY THEORY (G THEORY)

- ✘ A brief history
- ✘ Concepts and principles

Data structure

Facet-level sampling

Study focus

G coefficients

D studies

# A BRIEF HISTORY

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- ✘ Shortcomings of CTS model
  1. Ignoring the interaction of different sources of error
  2. No differentiation between systematic and unsystematic errors

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- ✘ Conceptual framework
    1. CTS based on classical correlational paradigm
    2. G theory based on ANOVA
  - ✘ Model symmetry (during the 1970s and 1980s)

Any factor as the object of measurement

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- ✘ Lee Cronbach as the originator of G theory
  - ✘ Cronbach, L. J., Gleser, G. C., Nanda, H., & Rajaratnam, N. (1972). *The dependability of behavioral measurements: Theory of generalizability for scores and profiles*. New York: Wiley.
  - ✘ Cronbach, L. J., Rajaratnam, N., & Gleser, G. C. (1963). Theory of generalizability: A liberalization of reliability theory. *British Journal of Mathematical and Statistical Psychology*, 16(2), 137–163.
  - ✘ In applied Linguistics:  
Bolus, R. E., Hinofotis, F. B., & Bailey, K. M. (1982). An introduction to generalizability in second language research. *Language Learning*, 32(2), 245-258.

# KEY TERMS

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- ✘ Facet:
- ✘ Condition:
- ✘ Universe score:
- ✘ Universe of admissible observations
- ✘ Universe of generalisation

# KEY CONCEPTS AND PRINCIPLES

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- ✘ Observation design
  1. Facets and their inter-relationships
    - a. Crossed designs
    - b. Nested designs
  2. Variance partitioning

# EXAMPLES OF DESIGN

## ✘ Examples of a crossed design

		Items				
		1	2	3	...	k
Students	1					
	2					
	...					
	n					

Grid illustrating the crossing of Students with Items (SI).

		Occasion			
		1		2	
Rater		1	2	1	2
Person	1				
	2				
	3				
	4				
	5				

# EXAMPLES OF A NESTED DESIGN

Methods	Method A					Method B				
Classes	1	2	3	4	5	6	7	8	9	10
Students										

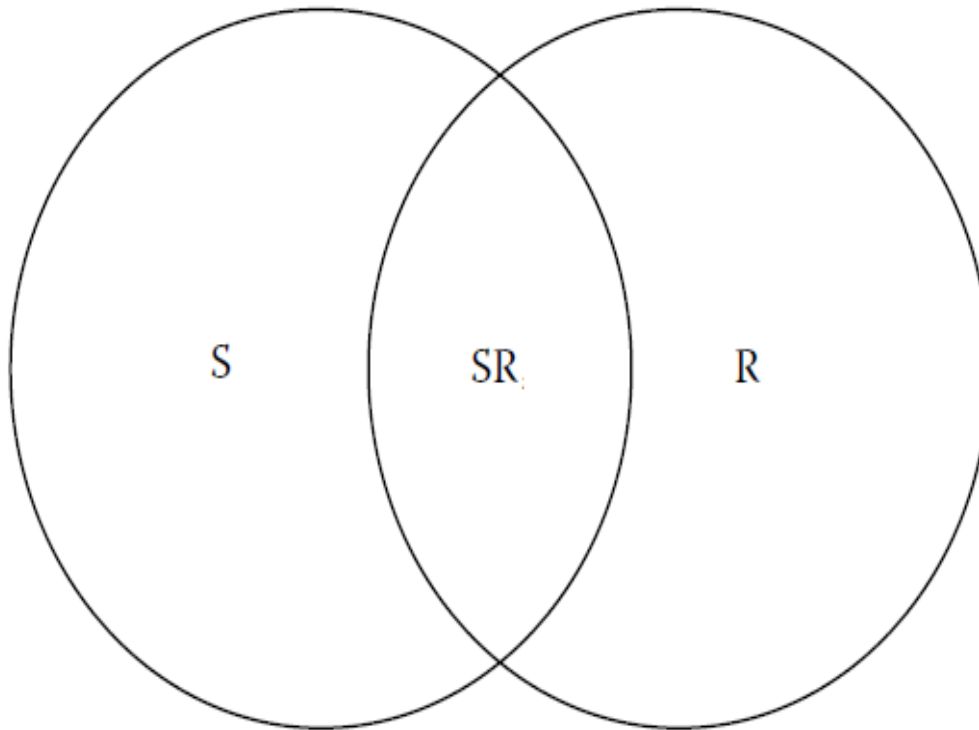
Grid illustrating the nesting of Students in Classes and in teaching Methods (S:C:M).

		Occasion			
		1		2	
Rater		1	2	3	4
	1				
	2				
Person	3				
	4				
	5				



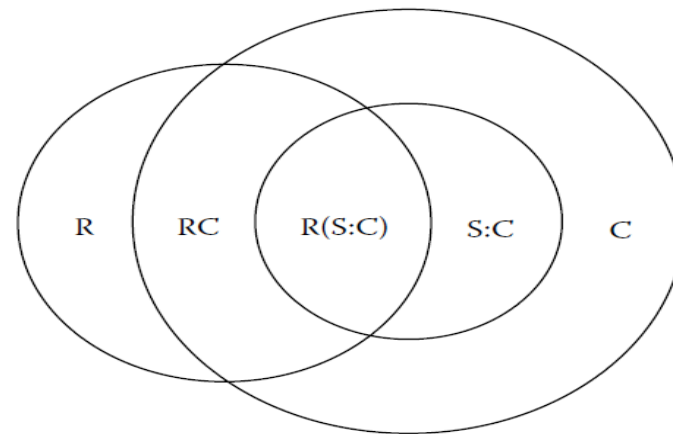
# EXAMPLES OF VARIANCE PARTITIONING

## ✘ Crossed designs

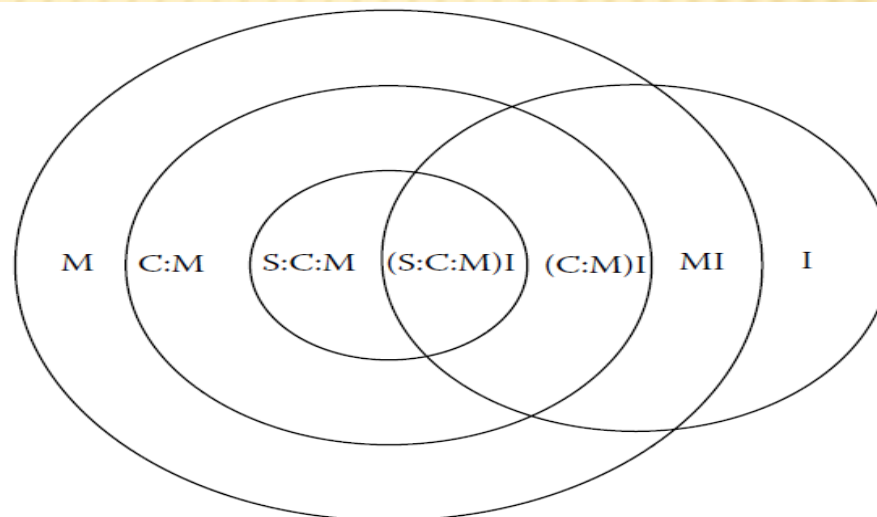


Variance partition diagram for the simplest model SR, where S and R represent Students and Raters, respectively,

# VARIANCE PARTITIONING FOR NESTED DESIGNS



Variance partition diagram for the model  $R(S:C)$ , where  $R$ ,  $S$ , and  $C$  represent Raters, Students, and Classes, respectively, and all facets are random.



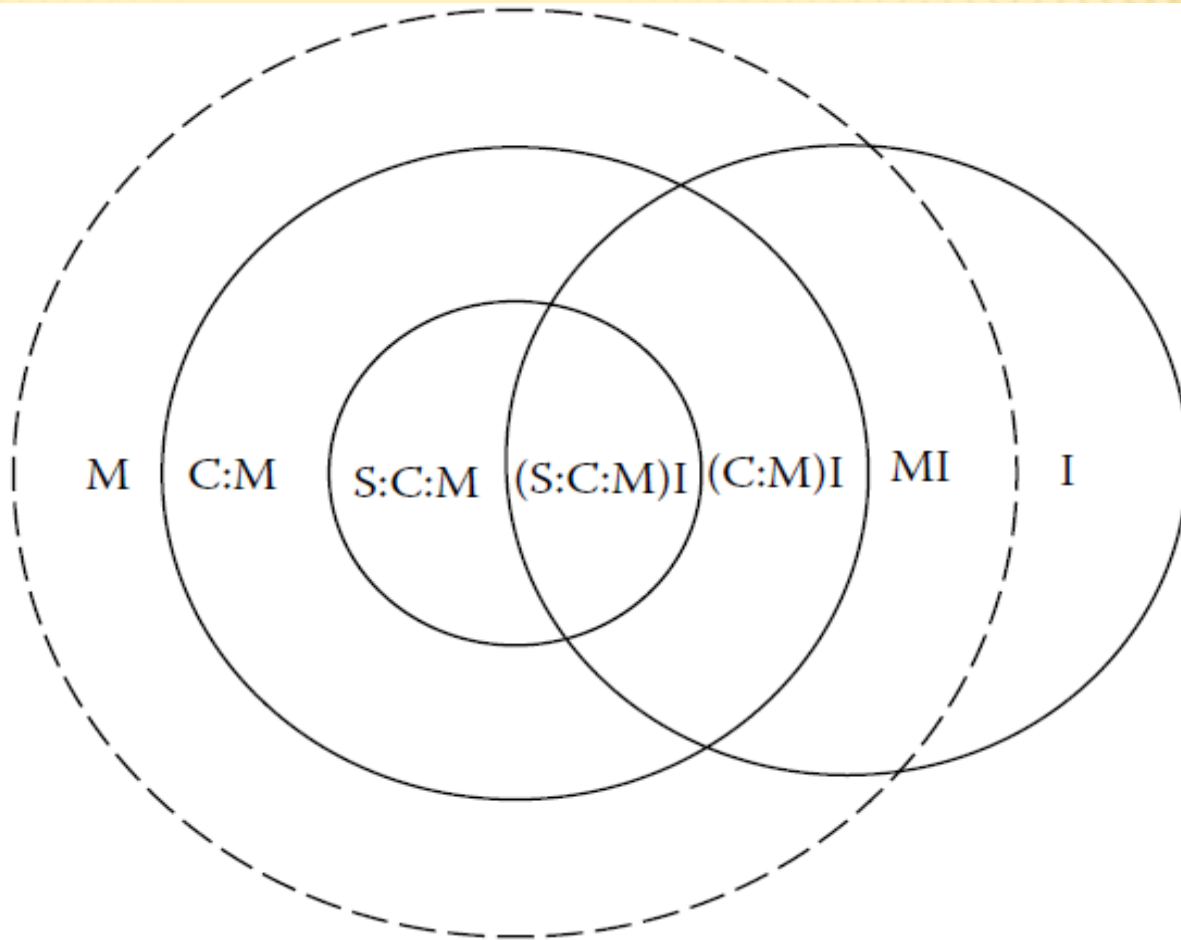
Variance partition diagram for the model  $(S:C:M)I$ , where  $S$ ,  $C$ ,  $M$ , and  $I$  represent Students, Classes, Methods, and Items, respectively

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✘ Estimation design (facet-level sampling)

1. Random facets
2. Purely random (infinite random) facets
3. Finite random facets
4. Fixed facets
5. Mixed facets

# AN EXAMPLE OF ESTIMATION DESIGN



Variance partition diagram for the estimation design  $(S:C:M)I$ , where  $S$ ,  $C$ ,  $M$ , and  $I$  represent Students, Classes, Methods, and Items, respectively,  $M$  is a fixed facet.

# MEASUREMENT DESIGN

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- ✘ Measurement design (study focus)
  1. Object of study
  2. Relative and absolute measurement

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## ✘ Design evaluation (G coefficients)

Four types of indices in G theory

1. generalizability coefficient
2. phi coefficient: dependability coefficient
3. absolute error variance
4. relative error variance

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✘ Optimization (D studies)

1. Changing the number of facets sampled
2. Eliminating atypical levels for certain facets
3. Changing the nature of facets

# WHAT IS GENERALIZABILITY THEORY?

- ✘ G theory is an approach to measurement precision which tries to identify various sources of variability and improve the measurement procedure.



<i>Sources of variation</i>	<i>VCS for G study</i> $n_t = 2 \text{ \& } n_r = 3$	<i>VCS for D study</i> $n_t = 2 \text{ \& } n_r = 1$	$n_t = 2 \text{ \& } n_r = 2$
$\sigma^2(p)$	0.149	0.149	0.149
$\sigma^2(t)$	0.000	0.000	0.000
$\sigma^2(r)$	0.000	0.000	0.000
$\sigma^2(pt)$	0.098	0.098	0.049
$\sigma^2(pr)$	0.015	0.015	0.008
$\sigma^2(tr)$	0.007	0.007	0.002
$\sigma^2(ptr)$	0.181	0.336	0.045
$\sigma^2 (\delta)$ relative error		0.290	0.102
$\sigma^2 (\Delta)$ absolute error		0.301	0.103
$E\rho^2$ G coefficient		0.336	0.594
$\hat{\Phi}$ phi coefficients		0.331	0.590